## Proofs III

Construct proofs for each of the following theorems using conditional proof or indirect proof. Use the generalpurpose proof form or do this on paper.

1. $\mathrm{A} \supset(\mathrm{B} \supset \mathrm{A})$
2. $(\mathrm{C} \supset \mathrm{D}) \equiv(\sim \mathrm{C} \vee \mathrm{D})$
3. $((\mathrm{A} \supset \mathrm{B}) \&(\mathrm{~B} \supset \mathrm{~A})) \supset(\mathrm{A} \equiv \mathrm{B})$
4. $(\mathrm{C} \equiv \sim \mathrm{D}) \supset \sim(\mathrm{C} \equiv \mathrm{D})$. This one isn't easy!
5. $\sim((\mathrm{A} \vee \sim \mathrm{A}) \supset(\mathrm{A} \& \sim \mathrm{~A}))$
6. $\sim(\mathrm{A} \& \sim \mathrm{~B}) \supset(\mathrm{A} \supset \mathrm{B})$
7. $\mathrm{A} \supset(\mathrm{A} \vee((\mathrm{B} \vee(\mathrm{C} \equiv \sim \mathrm{P})) \& \mathrm{Q}))$ This looks hard, but it's really easy!
8. $(\mathrm{E} \supset \mathrm{F}) \equiv \sim(\sim \mathrm{F} \& \mathrm{E})$
9. $((\sim \mathrm{R} v \mathrm{~S}) \&(\mathrm{~T} v \sim \mathrm{~S})) \supset(\sim \mathrm{T} \supset \sim \mathrm{R})$
10. $[(\mathrm{C} v \sim \mathrm{D}) \&(\sim \mathrm{C} \& \mathrm{D})] \supset[\mathrm{C} \equiv \sim(\mathrm{D} \& \sim \mathrm{C})]$
