BONUS QUIZ

Name:	
Date:	
Time Begun:	
Time Ended:	

Friday October 8 Ron Buckmire

Topic : Appreciating Quadratic Convergence

The idea behind this quiz is to give you an appreciation for the significance of quadratic convergence.

Reality Check:

EXPECTED SCORE : ____/10

ACTUAL SCORE : _____/10

Instructions:

- 1. Once you open the quiz, you have as much time as you need to complete it, but record your start time and end time at the top of this sheet.
- 2. You may use the book or any of your class notes. You must work alone.
- 3. If you use your own paper, please staple it to the quiz before coming to class. If you don't have a stapler, buy one.
- 4. After completing the quiz, sign the pledge below stating on your honor that you have adhered to these rules.
- 5. Your solutions must have enough details such that an impartial observer can read your work and determine HOW you came up with your solution.
- 6. Relax and enjoy...
- 7. This quiz is due on Monday October 11, in class. NO LATE QUIZZES WILL BE ACCEPTED.

Pledge: I, ______, pledge my honor as a human being and Occidental student, that I have followed all the rules above to the letter and in spirit.

Numerical Analysis

- 1. Consider the following sequences $p_{n+1} = 0.5p_n$ and $q_{n+1} = 0.5q_n^2$, which are linearly convergent and quadratically convergent, respectively.
- (a) [4 pts] Show that one can write expressions for the sequences in terms of the index n; that is, $p_n = \frac{1}{2^n}$ and $q_n = \frac{1}{2^{2^n-1}}$

(b) [4 pts] Derive expressions which show how many steps it takes for each sequence to be within ϵ of their limit $\lim_{n \to \infty} q_n = \lim_{n \to \infty} p_n = 0$

(c) [2 pts] Use your answer in part (b) to show how many steps it takes to reach a tolerance of 9 decimal places ($\epsilon = 5 \times 10^{-10}$).