Overview

- Basic MATLAB Operations
  - Starting MATLAB
  - Using MATLAB as a calculator
  - Introduction to variables and functions
- Matrices and Vectors: All variables are matrices.
  - Creating matrices and vectors
  - Subscript notation
  - Colon notation
- Additional Types of Variables
  - Complex numbers
  - Strings
  - Polynomials
- Working with Matrices and Vectors
  - Linear algebra
  - Vectorized operations
  - Array operators
- Managing the Interactive Environment
- Plotting

Starting MATLAB

- Double click on the MATLAB icon, or on unix systems type "matlab" at the command line.
- After startup MATLAB displays a command window that is used to enter commands and display text-only results.
- Enter Commands at the command prompt:
  - >> for full version
  - EDU for educational version
- MATLAB responds to commands by printing text in the command window, or by opening a figure window for graphical output.
- Toggle between windows by clicking on them with the mouse.

MATLAB Windows (version 5)
**Matlab Workspace (version 6)**

**Command Prompt:**
Enter typed commands here. Text results are displayed here.

**Recent Directory Menu:**
Used to change current working directory.

**Launch Pad/Workspace:**
Used to browse documentation, or view values of variables in the workspace.

**Command History/Current Directory:**
Used to view and re-enter typed commands, or change directories.

---

**Matlab as a Calculator**

Enter formulas at the command prompt

```
>> 2 + 6 - 4
ans =
4

>> ans/2
ans =
2
```

Or, define and use variables

```
>> a = 5
a =
5

>> b = 6
b =
6

>> c = b/a
c =
1.2000
```

---

**Built-in Variables**

- `pi` (= \(\pi\)) and `ans` are a built-in variables
  
  ```
  >> pi
  ans =
  3.1416
  >> sin(ans/4)
  ans =
  0.7071
  ```

  **Note:** There is no "degrees" mode. All angles are measured in radians.

---

**Built-in Functions**

Many standard mathematical functions, such as `sin`, `cos`, `log`, and `log10`, are built-in

```
>> log(256)
ans =
5.5452

>> log10(256)
ans =
2.4082

>> log2(256)
ans =
8
```
Looking for Functions

Syntax:

lookfor string

searches first line of function descriptions for "string".

Example:

>> lookfor cosine

produces

ACOS  Inverse cosine.
ACOSH Inverse hyperbolic cosine.
COS   Cosine.
COSH  Hyperbolic cosine.

On-line Help

Syntax:

help functionName

Example:

>> help log

produces

LOG   Natural logarithm.
LOG(X) is the natural logarithm of the elements of X.
Complex results are produced if X is not positive.
See also LOG2, LOG10, EXP, LOGM.

Ways to Get Help

• Use on-line help to request info on a specific function
  >> help sqrt

• The helpwin function opens a separate window for the help browser
  >> helpwin('sqrt')

• Use lookfor to find functions by keywords
  >> lookfor functionName

• In MATLAB version 6 and later the doc function opens the on-line version of the manual. This is very helpful for more complex commands.
  >> doc plot

Suppress Output with Semicolon

Results of intermediate steps can be suppressed with semicolons.

Example:

Assign values to x, y, and z, but only display the value of z in the command window:

>> x = 5;
>> y = sqrt(59);
>> z = log(y) + x^0.25
z =
 3.5341

Type variable name and omit the semicolon to print the value of a variable (that is already defined)

>> y
 y =
 7.6811 ( = log(sqrt(59)) + 5^0.25 )
Multiple Statements per Line

Use commas or semicolons to enter more than one statement at once. Commas allow multiple statements per line without suppressing output.

```
>> a = 5; b = sin(a), c = cosh(a)
b = -0.9589
>> c = 74.2099
```

Matlab Variables Names

Legal variable names:
- Begin with one of a–z or A–Z
- Have remaining characters chosen from a–z, A–Z, 0–9, or _
- Have a maximum length of 31 characters
- Should not be the name of a built-in variable, built-in function, or user-defined function

Examples:
```
xxxxxxxxx
pipeRadius
widgets_per_baubble
mySum
mysum
```

Note: mySum and mysum are different variables. Matlab is case sensitive.

Built-in Matlab Variables

<table>
<thead>
<tr>
<th>Name</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>ans</td>
<td>value of an expression when that expression is not assigned to a variable</td>
</tr>
<tr>
<td>eps</td>
<td>floating point precision</td>
</tr>
<tr>
<td>pi</td>
<td>( \pi ), ( 3.141492 \ldots )</td>
</tr>
<tr>
<td>realmax</td>
<td>largest positive floating point number</td>
</tr>
<tr>
<td>realmin</td>
<td>smallest positive floating point number</td>
</tr>
<tr>
<td>Inf</td>
<td>( \infty ), a number larger than realmax, the result of evaluating 1/0.</td>
</tr>
<tr>
<td>NaN</td>
<td>not a number, the result of evaluating 0/0</td>
</tr>
</tbody>
</table>

Rule: Only use built-in variables on the right hand side of an expression. Reassigning the value of a built-in variable can create problems with built-in functions.

Exception: i and j are preassigned to \( \sqrt{-1} \). One or both of i or j are often reassigned as loop indices. More on this later.

Matrices and Vectors

All Matlab variables are matrices

A Matlab vector is a matrix with one row or one column
A Matlab scalar is a matrix with one row and one column

Overview of Working with matrices and vectors
- Creating vectors: linspace and logspace
- Creating matrices: ones, zeros, eye, diag, ...
- Subscript notation
- Colon notation
- Vectorization
Creating **Matlab Variables**

**Matlab** variables are created with an assignment statement

\[ x = \text{expression} \]

where \( \text{expression} \) is a legal combinations of numerical values, mathematical operators, variables, and function calls that evaluates to a matrix, vector or scalar.

The expression can involve:

- Manual entry
- Built-in functions that return matrices
- Custom (user-written) functions that return matrices
- Loading matrices from text files or "mat" files

---

**Manual Entry**

For manual entry, the elements in a vector are enclosed in square brackets. When creating a row vector, separate elements with a space.

\[ v = \begin{bmatrix} 7 & 3 & 9 \end{bmatrix} \]

\( v = \begin{bmatrix} 7 & 3 & 9 \end{bmatrix} \)

Separate columns with a semicolon

\[ w = \begin{bmatrix} 2; 6; 1 \end{bmatrix} \]

\( w = \begin{bmatrix} 2 & 6 & 1 \end{bmatrix} \)

In a matrix, row elements are separated by spaces, and columns are separated by semicolons

\[ A = \begin{bmatrix} 1 & 2 & 3; 4 & 5 & 6; 7 & 8 & 9 \end{bmatrix} \]

\( A = \begin{bmatrix} 1 & 2 & 3; 4 & 5 & 6; 7 & 8 & 9 \end{bmatrix} \)

---

**Transpose Operator**

Once it is created, a variable can be transformed with other operators. The transpose operator converts a row vector to a column vector (and vice versa), and it changes the rows of a matrix to columns.

\[ v = \begin{bmatrix} 2 & 4 & 1 & 7 \end{bmatrix} \]

\( v = \begin{bmatrix} 2 & 4 & 1 & 7 \end{bmatrix} \)

\( v' \)

\[ A = \begin{bmatrix} 1 & 2 & 3; 4 & 5 & 6; 7 & 8 & 9 \end{bmatrix} \]

\( A = \begin{bmatrix} 1 & 2 & 3; 4 & 5 & 6; 7 & 8 & 9 \end{bmatrix} \)

\( A' \)

---

**Overwriting Variables**

Once a variable has been created, it can be reassigned

\[ x = 2; \]

\( x = 2; \)

\[ x = x + 2 \]

\( x = x + 2 \)

\( x = 4 \)

\( x = 4 \)

\[ y = \begin{bmatrix} 1 & 2 & 3 & 4 \end{bmatrix} \]

\( y = \begin{bmatrix} 1 & 2 & 3 & 4 \end{bmatrix} \)

\( y = y' \)

\( y = y' \)

\( y = \begin{bmatrix} 1 & 2 & 3 & 4 \end{bmatrix} \)

\( y = \begin{bmatrix} 1 & 2 & 3 & 4 \end{bmatrix} \)
Creating vectors with `linspace`

The `linspace` function creates vectors with elements having uniform linear spacing.

**Syntax:**
```
x = linspace(startValue, endValue)
x = linspace(startValue, endValue, nElements)
```

**Examples:**
```
>> u = linspace(0.0, 0.25, 5)
u =
     0    0.0625    0.1250    0.1875    0.2500
>> u = linspace(0.0, 0.25);
>> v = linspace(0, 9, 4)'
v =
     0
     3
     6
     9
```

**Note:** Column vectors are created by appending the transpose operator to `linspace`.

Creating vectors with `logspace`

The `logspace` function creates vectors with elements having uniform logarithmic spacing.

**Syntax:**
```
x = logspace(startValue, endValue)
x = logspace(startValue, endValue, nElements)
```

**Example:**
```
>> u = logspace(1, 4, 4)
u =
     10    100    1000   10000
```

Example: A Table of Trig Functions

```
>> x = linspace(0.2*pi, 6)';
>> y = sin(x);
>> z = cos(x);
>> [x y z]
ans =
     0     0   1.0000
   1.2566   0.9511   0.3090
   2.5133   0.5878  -0.8090
   3.7699  -0.5878  -0.8090
   5.0265  -0.9511   0.3090
   6.2832     0   1.0000
```

The expressions `y = sin(x)` and `z = cos(x)` take advantage of vectorization. If the input to a vectorized function is a vector or matrix, the output is often a vector or matrix having the same shape. More on this later.

Functions to Create Matrices (1)

<table>
<thead>
<tr>
<th>Name</th>
<th>Operation(s) Performed</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>diag</code></td>
<td>create a matrix with a specified diagonal entries,</td>
</tr>
<tr>
<td></td>
<td>or extract diagonal entries of a matrix</td>
</tr>
<tr>
<td><code>eye</code></td>
<td>create an identity matrix</td>
</tr>
<tr>
<td><code>ones</code></td>
<td>create a matrix filled with ones</td>
</tr>
<tr>
<td><code>rand</code></td>
<td>create a matrix filled with random numbers</td>
</tr>
<tr>
<td><code>zeros</code></td>
<td>create a matrix filled with zeros</td>
</tr>
<tr>
<td><code>linspace</code></td>
<td>create a row vector of linearly spaced elements</td>
</tr>
<tr>
<td><code>logspace</code></td>
<td>create a row vector of logarithmically spaced elements</td>
</tr>
</tbody>
</table>
Functions to Create Matrices (2)

Use `ones` and `zeros` to set initial values of a matrix or vector.

**Syntax:**

```matlab
A = ones(nrows, ncols)
A = zeros(nrows, ncols)
```

**Examples:**

```
>> D = ones(3,3)
D =
1 1 1
1 1 1
1 1 1
>> E = ones(2,4)
E =
1 1 1 1
1 1 1 1
```

Functions to Create Matrices (3)

`ones` and `zeros` are also used to create vectors. To do so, set either `nrows` or `ncols` to 1.

```
>> z = ones(1,4)
z =
1 1 1 1
>> t = zeros(3,1)
t =
0
0
0
```

Functions to Create Matrices (4)

The `eye` function creates identity matrices of a specified size. It can also create non-square matrices with ones on the main diagonal.

**Syntax:**

```matlab
A = eye(n)
A = eye(nrows, ncols)
```

**Examples:**

```
>> C = eye(5)
C =
1 0 0 0 0
0 1 0 0 0
0 0 1 0 0
0 0 0 1 0
0 0 0 0 1
>> D = eye(3,5)
D =
1 0 0 0 0
0 1 0 0 0
0 0 1 0 0
```

Functions to Create Matrices (5)

The `diag` function can either create a matrix with specified diagonal elements, or extract the diagonal elements from a matrix.

**Syntax:**

```matlab
A = diag(v)
v = diag(A)
```

**Example:**

Use `diag` to create a matrix

```
>> v = [1 2 3];
>> A = diag(v)
A =
1 0 0
0 2 0
0 0 3
```
Example:
Use `diag` to extract the diagonal of a matrix

```matlab
>> B = [1:4; 5:8; 9:12]
B=
1    2    3    4
5    6    7    8
9   10   11   12
>> w = diag(B)
w=
1
6
11
```

**Note:** The action of the `diag` function depends on the characteristics and number of the input(s). This polymorphic behavior of MATLAB functions is common. The on-line documentation (help `diag`) explains the possible variations.

---

**Subscript Notation (1)**

If `A` is a matrix, `A(i,j)` selects the element in the `i`th row and `j`th column. Subscript notation can be used on the right hand side of an expression to refer to a matrix element.

```matlab
>> A = [1 2 3; 4 5 6; 7 8 9];
>> b = A(3,2)
b =
8
>> c = A(1,1)
c =
1
```

Subscript notation is also used to assign matrix elements

```matlab
>> A(1,1) = c/b
A =
0.2500    2.0000    3.0000
4.0000    5.0000    6.0000
7.0000    8.0000    9.0000
```

---

**Subscript Notation (2)**

Referring to elements outside of current matrix dimensions results in an error

```matlab
>> A = [1 2 3; 4 5 6; 7 8 9];
>> A(1,4)
??? Index exceeds matrix dimensions.
```

Assigning an elements outside of current matrix dimensions causes the matrix to be resized!

```matlab
>> A = [1 2 3; 4 5 6; 7 8 9];
A =
1    2    3
4    5    6
7    8    9
>> A(4,4) = 11
A =
1    2    3    0
4    5    6    0
7    8    9    0
0    0    0    11
```

MATLAB automatically resizes matrices on the fly.

---

**Colon Notation (1)**

Colon notation is very powerful and very important in the effective use of MATLAB. The colon is used as both an operator and as a wildcard.

**Use colon notation to:**
- create vectors
- refer to or extract ranges of matrix elements

**Syntax:**

```
startValue:endValue
startValue:increment:endValue
```

**Note:** `startValue`, `increment`, and `endValue` do not need to be integers.
Colon Notation (1)

Creating row vectors:

```
>> s = 1:4
s =
    1    2    3    4
>> t = 0:0.1:0.4
 t =
    0   0.1000   0.2000   0.3000   0.4000
```

Creating column vectors:

```
>> u = (1:5)'
 u =
    1
    2
    3
    4
    5

>> v = 1:5'
 v =
    1    2    3    4    5
```

Colon notation is often used in compact expressions to obtain results that would otherwise require several steps.

Example:

```
>> A = ones(8,8);
>> A(3:6,3:6) = zeros(4,4)
 A =
    1    1    1    1    1    1    1
    1    1    1    1    1    1    1
    1    1    0    0    0    0    1
    1    1    0    0    0    0    1
    1    1    0    0    0    0    1
    1    1    1    1    1    1    1
    1    1    1    1    1    1    1
```

Colon Notation (2)

Colon Notation (3)

Use colon as a wildcard to refer to an entire column or row

```
>> A = [1 2 3; 4 5 6; 7 8 9];
>> A(:,1)
 ans =
    1
    4
    7
```

Or use colon notation to refer to subsets of columns or rows

```
>> A(2,:)  
 ans =
    4
    5
    6
```

Colon Notation (4)

Finally, colon notation is used to convert any vector or matrix to a column vector.

Examples:

```
>> x = 1:4;
>> y = x(:)
 y =
    1
    2
    3
    4
>> A = rand(2,3);
>> v = A(:)
 v =
    0.9501
    0.2311
    0.6068
    0.4860
    0.8913
    0.7621
    0.4565
    0.7919
```

Note: The rand function generates random elements between zero and one. Repeating the preceding statements will, in all likelihood, produce different numerical values for the elements of v.

Colon Notation (5)
Additional Types of Variables

The basic MATLAB variable is a matrix — a two dimensional array of values. The elements of a matrix variable can either be numeric values or characters. If the elements are numeric values they can either be real or complex (imaginary).

More general variable types are available: n-dimensional arrays (where $n > 2$), structs, cell arrays, and objects. Numeric (real and complex) and string arrays of dimension two or less will be sufficient for our purposes.

We now consider some simple variations on numeric and string matrices:

- Complex Numbers
- Strings
- Polynomials

Complex Numbers

MATLAB automatically performs complex arithmetic

$$\text{sqrt}(-4)$$
$$\text{ans} =$$
$$0 + 2.0000i$$

$$x = 1 + 2i$$
$$y = 1 - 2i$$

$$z = x * y$$
$$z = 5$$

Unit Imaginary Numbers

i and j are ordinary MATLAB variables that have be preassigned the value $\sqrt{-1}$.

```matlab
>> i^2
ans =
-1
```

Both or either i and j can be reassigned

```matlab
>> i = 5;
>> t = 8;
>> u = sqrt(i-t)
(u-t = -3, not -8+i)
ans =
0 + 1.7321i
>> u+w
ans =
-3.0000
```

Euler Notation (1)

Euler notation represents a complex number by a phaser

$$z = \zeta e^{i \theta}$$

$$x = \Re(z) = |z| \cos(\theta) = \zeta \cos(\theta)$$

$$y = i \Im(z) = i |z| \sin(\theta) = i \zeta \sin(\theta)$$
Functions for Complex Arithmetic (1)

<table>
<thead>
<tr>
<th>Function</th>
<th>Operation</th>
</tr>
</thead>
<tbody>
<tr>
<td>abs</td>
<td>Compute the magnitude of a number ( \text{abs}(z) ) is equivalent to ( \sqrt{\text{real}(z)^2 + \text{imag}(z)^2} )</td>
</tr>
<tr>
<td>angle</td>
<td>Angle of complex number in Euler notation</td>
</tr>
<tr>
<td>exp</td>
<td>If ( x ) is real, ( \exp(x) = e^x ) If ( z ) is complex, ( \exp(z) = e^{\text{Re}(z)(\cos(\text{Im}(z)) + i\sin(\text{Im}(z)))} )</td>
</tr>
<tr>
<td>conj</td>
<td>Complex conjugate of a number</td>
</tr>
<tr>
<td>imag</td>
<td>Extract the imaginary part of a complex number</td>
</tr>
<tr>
<td>real</td>
<td>Extract the real part of a complex number</td>
</tr>
</tbody>
</table>

Note: When working with complex numbers, it is a good idea to reserve either \( i \) or \( j \) for the unit imaginary value \( \sqrt{-1} \).

Examples:

```matlab
>> zeta = 5; theta = pi/3;
>> z = zeta*exp(i*theta)
    z =
    2.5000 + 4.3301i
>> abs(z)
    ans =
    5
>> sqrt(z*conj(z))
    ans =
    5
>> x = real(z)
    x =
    2.5000
>> y = imag(z)
    y =
    4.3301
>> angle(z)*180/pi
    ans =
    60.0000
```

Remember: There is no “degrees” mode in Matlab. All angles are measured in radians.

Strings

- Strings are matrices with character elements.
- String constants are enclosed in single quotes
- Colon notation and subscript operations apply

Examples:

```matlab
>> first = 'John';
>> last = 'Coltrane';
>> name = [first,' ',last]
   name =
   John Coltrane
>> length(name)
   ans =
   13
>> name(9:13)
   ans =
   trane
```

Functions for String Manipulation (1)

<table>
<thead>
<tr>
<th>Function</th>
<th>Operation</th>
</tr>
</thead>
<tbody>
<tr>
<td>char</td>
<td>convert an integer to the character using ASCII codes, or combine characters into a character matrix</td>
</tr>
<tr>
<td>findstr</td>
<td>finds one string in another string</td>
</tr>
<tr>
<td>length</td>
<td>returns the number of characters in a string</td>
</tr>
<tr>
<td>num2str</td>
<td>converts a number to string</td>
</tr>
<tr>
<td>str2num</td>
<td>converts a string to a number</td>
</tr>
<tr>
<td>strcmp</td>
<td>compares two strings</td>
</tr>
<tr>
<td>strmatch</td>
<td>identifies rows of a character array that begin with a string</td>
</tr>
<tr>
<td>strncmp</td>
<td>compares the first ( n ) elements of two strings</td>
</tr>
<tr>
<td>sprintf</td>
<td>converts strings and numeric values to a string</td>
</tr>
</tbody>
</table>
Functions for String Manipulation (2)

Examples:

```matlab
>> msg1 = ['There are ',num2str(100/2.54),' inches in a meter']
msg1 =
There are 39.3701 inches in a meter

>> msg2 = sprintf('There are %5.2f cubic inches in a liter',1000/2.54^3)
msg2 =
There are 61.02 cubic inches in a liter

>> both = char(msg1,msg2)
both =
There are 39.3701 inches in a meter
There are 61.02 cubic inches in a liter

>> strcmp(msg1,msg2)
an =
0

>> strncmp(msg1,msg2,9)
an =
1

>> findstr('in',msg1)
an =
19 26
```

Polynomials

MATLAB polynomials are stored as vectors of coefficients. The polynomial coefficients are stored in decreasing powers of x:

\[ P_n(x) = c_1x^n + c_2x^{n-1} + \ldots + c_n x + c_{n+1} \]

Example:

Evaluate \( x^3 - 2x + 12 \) at \( x = -1.5 \)

```matlab
>> c = [1 0 -2 12];
>> polyval(c,-1.5)
an =
12.3750
```

Functions for Manipulating Polynomials

<table>
<thead>
<tr>
<th>Function</th>
<th>Operations performed</th>
</tr>
</thead>
<tbody>
<tr>
<td>conv</td>
<td>product (convolution) of two polynomials</td>
</tr>
<tr>
<td>deconv</td>
<td>division (deconvolution) of two polynomials</td>
</tr>
<tr>
<td>poly</td>
<td>Create a polynomial having specified roots</td>
</tr>
<tr>
<td>polyder</td>
<td>Differentiate a polynomial</td>
</tr>
<tr>
<td>polyval</td>
<td>Evaluate a polynomial</td>
</tr>
<tr>
<td>polyfit</td>
<td>Polynomial curve fit</td>
</tr>
<tr>
<td>roots</td>
<td>Find roots of a polynomial</td>
</tr>
</tbody>
</table>

Manipulation of Matrices and Vectors

The name "MATLAB" evolved as an abbreviation of "MATrix LABoratory". The data types and syntax used by MATLAB make it easy to perform the standard operations of linear algebra including addition and subtraction, multiplication of vectors and matrices, and solving linear systems of equations.

Chapter 7 provides a detailed review of linear algebra. Here we provide a simple introduction to some operations that are necessary for routine calculation.

- Vector addition and subtraction
- Inner and outer products
- Vectorization
- Array operators
Vector Addition and Subtraction

Vector and addition and subtraction are element-by-element operations.

Example:

```
>> u = [10 9 8]; (u and v are row vectors)
>> v = [1 2 3];
>> u+v
ans =
    11 11 11
>> u-v
ans =
     9   7   5
```

Vector Inner and Outer Products

The inner product combines two vectors to form a scalar

\[ \sigma = u \cdot v = u^T v \iff \sigma = \sum u_i v_i \]

The outer product combines two vectors to form a matrix

\[ A = u^T v \iff a_{ij} = u_i v_j \]

Inner and Outer Products in MATLAB

Inner and outer products are supported in MATLAB as natural extensions of the multiplication operator

```
>> u = [10 9 8]; (u and v are row vectors)
>> v = [1 2 3];
>> u*v'
ans =
    52
>> u'*v
ans =
   30  18  10
   16  12  27
```

Vectorization

- **Vectorization** is the use of single, compact expressions that operate on all elements of a vector without explicitly executing a loop. The loop is executed by the MATLAB kernel, which is much more efficient at looping than interpreted MATLAB code.
- Vectorization allows calculations to be expressed succinctly so that programmers get a high level (as opposed to detailed) view of the operations being performed.
- Vectorization is important to make MATLAB operate efficiently.
Vectorization of Built-in Functions

Most built-in function support vectorized operations. If the input is a scalar the result is a scalar. If the input is a vector or matrix, the output is a vector or matrix with the same number of rows and columns as the input.

Example:

```matlab
>> x = 0:pi/4:pi    % define a row vector
   x =
        0    0.7854    1.5708    2.3562    3.1416
>> y = cos(x)     % evaluate cosine of each x(i)
   y =
        1.0000    0.7071          0   -0.7071   -1.0000
```

Contrast with Fortran implementation:

```fortran
real x(5),y(5)
pi = 3.14159624
dx = pi/4.0
do 10 i=1,5
   x(i) = (i-1)*dx
   y(i) = sin(x(i))
10 continue
```

No explicit loop is necessary in MATLAB.

Array Operators

Array operators support element-by-element operations that are not defined by the rules of linear algebra.

Array operators are designated by a period prepended to the standard operator.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Operation</th>
</tr>
</thead>
<tbody>
<tr>
<td>.*</td>
<td>element-by-element multiplication</td>
</tr>
<tr>
<td>./</td>
<td>element-by-element &quot;right&quot; division</td>
</tr>
<tr>
<td>.\</td>
<td>element-by-element &quot;left&quot; division</td>
</tr>
<tr>
<td>.^</td>
<td>element-by-element exponentiation</td>
</tr>
</tbody>
</table>

Array operators are a very important tool for writing vectorized code.

Using Array Operators (1)

Examples:

Element-by-element multiplication and division

```matlab
>> u = [1 2 3];
>> v = [4 5 6];
>> w = u.*v        % element-by-element product
   w =
        4    10    18
>> x = u./v        % element-by-element division
   x =
        0.2500    0.4000    0.5000
>> y = sin(pi*u/2) .* cos(pi*v/2)
   y =
        1    0    1
>> z = sin(pi*u/2) ./ cos(pi*v/2)
   Warning: Divide by zero.
   z =
        1   NaN    1
```
Using Array Operators (2)

Examples:

Application to matrices

```
>> A = [ 1 2 3 4; 5 6 7 8 ];
>> B = [ 8 7 6 5; 4 3 2 1 ];
>> A.*B
ans =
 8 14 18 20
20 18 14 8
>> A*B
??? Error using ==> *
Inner matrix dimensions must agree.
>> A*B'
ans =
 60 20
164 60
>> A.'^2
ans =
  1  4  9 16
 25 36 49 64
```
Working with External Data Files

Write data to a file

```matlab
save fileName
save fileName variable1 variable2 ...
save fileName variable1 variable2 ... -ascii
```

Read in data stored in matrices

```matlab
load fileName
load fileName matrixVariable
```

Loading Data from External File

Example:

```matlab
Load data from a file and plot the data

>> load wolfSun.dat;
>> xdata = wolfSun(:,1);
>> ydata = wolfSun(:,2);
>> plot(xdata,ydata)
```

The Matlab Path

Matlab will only use those functions and data files that are in its path.

To add N:\IMAUSER\ME352\PS2 to the path, type

```matlab
>> p = path;
>> path(p,'N:\IMAUSER\ME352\PS2');
```

Matlab version 5 and later has an interactive path editor that makes it easy to adjust the path.

The path specification string depends on the operating system. On a Unix/Linux computer a path setting operation might look like:

```matlab
>> p = path;
>> path(p,'~/matlab/ME352/ps2');
```

Plotting

- Plotting (x, y) data
- Axis scaling and annotation
- 2D (contour) and 3D (surface) plotting
Two dimensional plots are created with the **plot** function.

**Syntax:**

```matlab
plot(x,y)
plot(xdata,ydata,symbol)
plot(x1,y1,x2,y2,...)
plot(x1,y1,symbol1,x2,y2,symbol2,...)
```

**Note:** $x$ and $y$ must have the same shape, $x_1$ and $y_1$ must have the same shape, $x_2$ and $y_2$ must have the same shape, etc.

### Line and Symbol Types (1)

The curves for a data set are drawn from combinations of the color, symbol, and line types in the following table.

<table>
<thead>
<tr>
<th>Color</th>
<th>Symbol</th>
<th>Line</th>
</tr>
</thead>
<tbody>
<tr>
<td>y</td>
<td>yellow</td>
<td>solid</td>
</tr>
<tr>
<td>m</td>
<td>magenta</td>
<td>dotted</td>
</tr>
<tr>
<td>c</td>
<td>cyan</td>
<td>dashdot</td>
</tr>
<tr>
<td>r</td>
<td>red</td>
<td>dashed</td>
</tr>
<tr>
<td>g</td>
<td>green</td>
<td></td>
</tr>
<tr>
<td>b</td>
<td>blue</td>
<td></td>
</tr>
<tr>
<td>w</td>
<td>white</td>
<td></td>
</tr>
<tr>
<td>k</td>
<td>black</td>
<td></td>
</tr>
<tr>
<td>.</td>
<td>point</td>
<td></td>
</tr>
<tr>
<td>o</td>
<td>circle</td>
<td></td>
</tr>
<tr>
<td>x</td>
<td>x-mark</td>
<td></td>
</tr>
<tr>
<td>+</td>
<td>plus</td>
<td></td>
</tr>
<tr>
<td>*</td>
<td>star</td>
<td></td>
</tr>
<tr>
<td>s</td>
<td>square</td>
<td></td>
</tr>
<tr>
<td>d</td>
<td>diamond</td>
<td></td>
</tr>
<tr>
<td>v</td>
<td>triangle</td>
<td>(down)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>triangle (up)</td>
</tr>
<tr>
<td>&lt;</td>
<td>triangle</td>
<td>(left)</td>
</tr>
<tr>
<td>&gt;</td>
<td>triangle</td>
<td>(right)</td>
</tr>
<tr>
<td>p</td>
<td>pentagram</td>
<td></td>
</tr>
<tr>
<td>h</td>
<td>hexagram</td>
<td></td>
</tr>
</tbody>
</table>

To choose a color/symbol/line style, chose one entry from each column.

### Line and Symbol Types (2)

Examples:

Put yellow circles at the data points:

```matlab
plot(x,y,'yo')
```

Plot a red dashed line with no symbols:

```matlab
plot(x,y,'r--')
```

Put black diamonds at each data point and connect the diamonds with black dashed lines:

```matlab
plot(x,y,'kd--')
```
Alternative Axis Scaling (1)

Combinations of linear and logarithmic scaling are obtained with functions that, other than their name, have the same syntax as the plot function.

<table>
<thead>
<tr>
<th>Name</th>
<th>Axis scaling</th>
</tr>
</thead>
<tbody>
<tr>
<td>loglog</td>
<td>( \log_{10}(y) ) versus ( \log_{10}(x) )</td>
</tr>
<tr>
<td>plot</td>
<td>linear ( y ) versus ( x )</td>
</tr>
<tr>
<td>semilogx</td>
<td>linear ( y ) versus ( \log_{10}(x) )</td>
</tr>
<tr>
<td>semilogy</td>
<td>( \log_{10}(y) ) versus linear ( x )</td>
</tr>
</tbody>
</table>

Note: As expected, use of logarithmic axis scaling for data sets with negative or zero values results in an error. MATLAB will complain and then plot only the positive (nonzero) data.

Example:

```matlab
g = linspace(0,3);
y = 10*exp(-2*x);
plot(x,y);
semilogy(x,y);
```

Multiple plots per figure window (1)

The subplot function is used to create a matrix of plots in a single figure window.

Syntax:

```
subplot(nrows,ncols,thisPlot)
```

Repeat the values of `nrows` and `ncols` for all plots in a single figure window. Increment `thisPlot` for each plot.

Example:

```matlab
>> x = linspace(0,2*pi);
>> subplot(2,2,1);
>> plot(x,sin(x)); axis([0 2*pi -1.5 1.5]); title('sin(x)');
>> subplot(2,2,2);
>> plot(x,sin(2*x)); axis([0 2*pi -1.5 1.5]); title('sin(2x)');
>> subplot(2,2,3);
>> plot(x,sin(3*x)); axis([0 2*pi -1.5 1.5]); title('sin(3x)');
>> subplot(2,2,4);
>> plot(x,sin(4*x)); axis([0 2*pi -1.5 1.5]); title('sin(4x)');
```

(See next slide for the plot.)

Multiple plots per figure window (2)
Plot Annotation

<table>
<thead>
<tr>
<th>Name</th>
<th>Operation(s) performed</th>
</tr>
</thead>
<tbody>
<tr>
<td>axis</td>
<td>Reset axis limits</td>
</tr>
<tr>
<td>grid</td>
<td>Draw grid lines corresponiding to the major major ticks on the x and y axes</td>
</tr>
<tr>
<td>gtext</td>
<td>Add text to a location determined by a mouse click</td>
</tr>
<tr>
<td>legend</td>
<td>Create a legend to identify symbols and line types when multiple curves are drawn on the same plot</td>
</tr>
<tr>
<td>text</td>
<td>Add text to a specified (x, y) location</td>
</tr>
<tr>
<td>xlabel</td>
<td>Label the x-axis</td>
</tr>
<tr>
<td>ylabel</td>
<td>Label the y-axis</td>
</tr>
<tr>
<td>title</td>
<td>Add a title above the plot</td>
</tr>
</tbody>
</table>

Plot Annotation Example

```matlab
>> D = load('pdxTemp.dat'); m = D(:,1); T = D(:,2:4);
>> plot(m,t(:,1),'ro',m,T(:,2),'k+',m,T(:,3),'b-');
>> xlabel('Month');
>> ylabel('Temperature (\circ F)');
>> title('Monthly average temperature at PDX');
>> axis([1 12 20 100]);
>> legend('High','Low','Average',2);
```

Note: The `pdxTemp.dat` file is in the data directory of the NMM toolbox. Make sure the toolbox is installed and is included in the MATLAB path.