

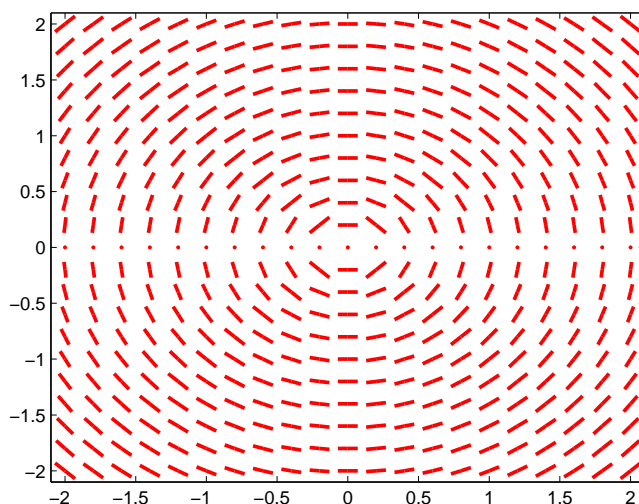


## Slope Fields and Euler's Method

### Exercise

Consider the differential equation  $y' = -x/y$  with initial condition  $y(0) = 1$ . Given that the exact solution is  $y(x) = \sqrt{1-x^2}$ ,

- use the slope field to estimate  $y(1/2)$  for the solution that satisfies the given initial condition.
- Compare your estimate with the exact value of  $y(1/2)$
- Use Euler's Method with  $\Delta x = .25$  to estimate  $y(1/2)$ .
- Is your Euler's Method estimate and over-estimate or under-estimate? Explain why.



To use Euler's Method generally the following table can be helpful

$x$	$y$	$y'$	$\Delta y$

## Numerical Error in Using Euler's Method

### GROUPWORK

Complete the following sentences:

As the time step  $\Delta t$  \_\_\_\_\_ in magnitude, the numerical error in computing  $y(x_0)$  using Euler's Method decreases in magnitude.

As the time step  $\Delta t$  \_\_\_\_\_ in magnitude, the numerical error in computing  $y(x_0)$  using Euler's Method increases in magnitude.

When  $y''$  is \_\_\_\_\_ on  $x_0 < x < x_1$  the function  $y(x)$  is concave up and estimates of  $y(x_1)$  using Euler's Method will be \_\_\_\_\_.

When  $y''$  is \_\_\_\_\_ on  $x_0 < x < x_1$  the function  $y(x)$  is concave down and estimates of  $y(x_1)$  using Euler's Method will be \_\_\_\_\_.