Quiz  $\mathbf{8}$ 

Name: \_\_\_\_\_

Time Begun:	
Time Ended:	

Monday November 24 Ron Buckmire

Topic : Advanced Laplace Transforms

The idea behind this quiz is to provide you with an opportunity to demonstrate your ability with inverting Laplace Transforms of a complicated function.

## Reality Check:

EXPECTED SCORE : \_\_\_\_/10

ACTUAL SCORE : \_\_\_\_/10

## Instructions:

- 0. Please look for a hint on this quiz posted to faculty.oxy.edu/ron/math/341/08/
- 1. Once you open the quiz, you have **30 minutes** to complete, please record your start time and end time at the top of this sheet.
- 2. You may use the book or any of your class notes. You must work alone.
- 3. If you use your own paper, please staple it to the quiz before coming to class. If you don't have a stapler, buy one. QUIZZES WITH UNSTAPLED SHEETS WILL NOT BE GRADED.
- 4. After completing the quiz, sign the pledge below stating on your honor that you have adhered to these rules.
- 5. Your solutions must have enough details such that an impartial observer can read your work and determine HOW you came up with your solution.
- 6. Relax and enjoy...
- 7. This quiz is due on Monday December 1, at the beginning of class. NO LATE OR UNSTAPLED QUIZZES WILL BE ACCEPTED.

**Pledge:** I, \_\_\_\_\_, pledge my honor as a human being and Occidental student, that I have followed all the rules above to the letter and in spirit.

DIFFERENTIAL EQUATIONS

Math 341 Fall 2008

## SHOW ALL YOUR WORK

Quiz EIGHT

1. We're interested in finding the function f(t) whose Laplace Transform is

$$F(s) = A(s) - B(s) = \frac{1}{s^2} - \frac{e^{-s}}{s(1 - e^{-s})}, \quad s > 0$$

(a) 2 points. Compute  $\mathcal{L}^{-1}\left[\frac{1}{s^2}\right] = a(t)$ .

(b) 2 points. If one considers  $\frac{1}{1-e^{-s}}$  as the sum of a geometric series  $\sum_{k=0}^{\infty} ar^k$  with first term a = 1 and ratio  $r = e^{-s}$  then show that  $\frac{e^{-s}}{s(1-e^{-s})}$  can be written as  $\sum_{k=1}^{\infty} \frac{e^{-ks}}{s} = \frac{e^{-s}}{s} + \frac{e^{-2s}}{s} + \frac{e^{-3s}}{s} + \dots$ 

(c) 3 points. Recall that  $\mathcal{L}^{-1}[e^{-as}F(s)] = f(t-a)\mathcal{H}(t-a)$ . Using the result given in (b), compute  $\mathcal{L}^{-1}\left[\frac{e^{-s}}{s(1-e^{-s})}\right] = b(t).$ 

(d) 3 points. Give a sketch of a(t), b(t) and f(t) = a(t) - b(t) below for t > 0 (Use different pairs of axes for each graph.)