Name: $\qquad$

Time Begun: $\qquad$
Friday October 24
Ron Buckmire
Time Ended: $\qquad$

## Topic : Bifurcations in Systems of Differential Equations

The idea behind this quiz is to provide you with an opportunity to think about how bifurcations can occur in linear systems of DEs.

## Reality Check:

EXPECTED SCORE : $\qquad$ /10

ACTUAL SCORE : $\qquad$ /10

## Instructions:

0. Please look for a hint on this quiz posted to faculty.oxy.edu/ron/math/341/08/
1. Once you open the quiz, you have $\mathbf{3 0}$ minutes to complete, please record your start time and end time at the top of this sheet.
2. You may use the book or any of your class notes. You must work alone.
3. If you use your own paper, please staple it to the quiz before coming to class. If you don't have a stapler, buy one. QUIZZES WITH UNSTAPLED SHEETS WILL NOT BE GRADED.
4. After completing the quiz, sign the pledge below stating on your honor that you have adhered to these rules.
5. Your solutions must have enough details such that an impartial observer can read your work and determine HOW you came up with your solution.
6. Relax and enjoy...
7. This quiz is due on Monday October 27, at the beginning of class. NO LATE OR UNSTAPLED QUIZZES WILL BE ACCEPTED.

Pledge: I, $\qquad$ , pledge my honor as a human being and Occidental student, that I have followed all the rules above to the letter and in spirit.

1. Consider the linear system of ordinary differential equations with a parameter $a$

$$
\frac{d \vec{x}}{d t}=\left[\begin{array}{ll}
2 & a \\
2 & 0
\end{array}\right] \vec{x} \text { where } \vec{x}(t)=\left[\begin{array}{l}
x(t) \\
y(t)
\end{array}\right]
$$

Let's describe how the phase portrait changes as $a$ varies from $-\infty$ to $+\infty$.
(a) 3 points. Compute all the eigenvalues and eigenvectors in order to sketch the phase portrait when $a=-3 / 2$. Describe the stationary point at the origin.
(b) 3 points. Compute all the eigenvalues and eigenvectors in order to sketch the phase portrait when $a=1$. Describe the stationary point at the origin.
(c) 4 points. For what value of $a$ does the system change its nature (i.e. bifurcate)? For this value of $a$, compute the eigenvalues and eigenvectors in order to sketch the phase portrait. Describe the stationary point at the origin.

