Quiz  $\mathbf{4}$ 

Name: \_\_\_\_\_

Time Begun:	
Time Ended:	

**Topic** : Visualizing Solutions of Linear Systems of ODEs

The idea behind this quiz is to provide you with an opportunity to illustrate your understanding of solution techniques for systems of n linear ordinary differential equations.

## Reality Check:

EXPECTED SCORE : \_\_\_\_/10

ACTUAL SCORE : \_\_\_\_/10

## Instructions:

- 0. Please look for a hint on this quiz posted to faculty.oxy.edu/ron/math/341/08/
- 1. Once you open the quiz, you have **30 minutes** to complete, please record your start time and end time at the top of this sheet.
- 2. You may use the book or any of your class notes. You must work alone.
- 3. If you use your own paper, please staple it to the quiz before coming to class. If you don't have a stapler, buy one. QUIZZES WITH UNSTAPLED SHEETS WILL NOT BE GRADED.
- 4. After completing the quiz, sign the pledge below stating on your honor that you have adhered to these rules.
- 5. Your solutions must have enough details such that an impartial observer can read your work and determine HOW you came up with your solution.
- 6. Relax and enjoy...
- 7. This quiz is due on Wednesday October 15, at the beginning of class. NO LATE OR UNSTAPLED QUIZZES WILL BE ACCEPTED.

**Pledge:** I, \_\_\_\_\_, pledge my honor as a human being and Occidental student, that I have followed all the rules above to the letter and in spirit.

## **Differential Equations**

Friday October 10 Ron Buckmire

## SHOW ALL YOUR WORK

1. Consider the system of ordinary differential equations

$$\frac{d\vec{x}}{dt} = A\vec{x} = \begin{bmatrix} 0 & 2\\ 0 & -1 \end{bmatrix} \vec{x} \text{ where } \vec{x}(t) = \begin{bmatrix} x(t)\\ y(t) \end{bmatrix}$$

(a) 4 points. Show that the matrix A has eigenvalues 0 and -1 and eigenvectors which are multiples of  $\begin{bmatrix} 1\\0 \end{bmatrix}$  and  $\begin{bmatrix} -2\\1 \end{bmatrix}$ . Write down the 2-parameter general solution of the system  $\frac{d\vec{x}}{dt} = A\vec{x}$ .

(b) 3 points. Find the exact solution  $\vec{x}(t)$  for each of the trajectories which go through the points A(1,1), B(0,-2) and C(4,0) at t = 0.

(c) 3 points. On the figure below clearly indicate the trajectories for each of the solutions which start at  $\mathbf{A}(1,1)$ ,  $\mathbf{B}(0,-2)$  and  $\mathbf{C}(4,0)$  ends up as  $t \to \infty$ . Label these endpoints  $\mathbf{A}'$ ,  $\mathbf{B}'$  and  $\mathbf{C}'$  respectively.

