| Quiz 8 | Linear Systems |
|---|---|
| Name: | |
| Date: | Friday March 31 Ron Buckmire |
| $f{Topic}$: Diagonalization of a Matrix and its Impl | ications for Matrix Exponentiation |
| The idea behind this quiz is for you to indicate your under and eigenvectors associated with a matrix to computing | |
| Reality Check: | |
| EXPECTED SCORE :/10 | ACTUAL SCORE :/10 |
| Instructions: | |
| 1. Please look for a hint on this quiz posted to fa | culty.oxy.edu/ron/math/214/06/ |
| 2. You may use the book or any of your class note | es. You must work alone. |
| 3. If you use your own paper, please staple it to the a stapler, buy one. QUIZZES WITH UNSTAP | - • |
| 4. After completing the quiz, sign the pledge below to these rules. | stating on your honor that you have adhered |
| 5. Your solutions must have enough details such t and determine HOW you came up with your so | |
| 6. Relax and enjoy | |
| 7. This quiz is due on Monday April 3, in cl WILL BE ACCEPTED. | ass. NO LATE OR UNSTAPLED QUIZZES |
| Pledge: I,, pledge my hothat I have followed all the rules above to the letter a | |

- **1.** Consider the matrix $A = \begin{bmatrix} 1/2 & 1/2 \\ 1 & 0 \end{bmatrix}$. We want to obtain a value for $A^{\infty} = \lim_{n \to \infty} A^n$.
- **a.** (4 points). Find the eigenvalues and eigenvectors of A.

b. (2 points) Show that $AS = S\Lambda$ or $A = S\Lambda S^{-1}$, where the columns of S are formed by the eigenvectors of A and Λ is a diagonal matrix with the eigenvalues of A along the diagonal and zeroes elsewhere.

c. (2 points). Compute $A^n = S\Lambda^n S^{-1}$.

d. (2 points). Use your answer from **c** to show that $A^{\infty} = \begin{bmatrix} 2/3 & 1/3 \\ 2/3 & 1/3 \end{bmatrix}$.