

The Case for Quantitative Literacy

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he world of the twenty-first century is a world awash in numbers. Headlines use quantitative measures to report increases in gasoline prices, changes in SAT scores, risks of dying from colon cancer, and numbers of refugees from the latest ethnic war. Advertisements use numbers to compete over costs of cell phone contracts and low-interest car loans. Sports reporting abounds in team statistics and odds on forth-coming competitions.

More important for many people are the rapidly increasing uses of quantitative thinking in the workplace, in education, and in nearly every other field of human endeavor. Farmers use computers to find markets, analyze soil, and deliver controlled amounts of seeds and nutrients; nurses use unit conversions to verify accuracy of drug dosages; sociologists draw inferences from data to understand human behavior; biologists develop computer algorithms to map the human genome; factory supervisors use "six-sigma" strategies to ensure quality control; entrepreneurs project markets and costs using computer spreadsheets; lawyers use statistical evidence and arguments involving probabilities to convince jurors. The roles played by numbers and data in contemporary society are virtually endless.

Unfortunately, despite years of study and life experience in an environment immersed in data, many educated adults remain functionally innumerate. Most U.S. students leave high school with quantitative skills far below what they need to live well in today's society; businesses lament

show that the average mathematics performance of seventeen-year-old virtually every college finds that many students need remedial mathematthe lack of technical and quantitative skills of prospective employees; and students has risen just one percent in 25 years and remains, at 307, in the ics. Data from the National Assessment of Educational Progress (NAEP) age scores of Hispanic students (292) and black students (286) are near range (336-367). Moreover, despite slight growth in recent years, averlower half of the "basic" range (286-336) and well below the "proficient"

graduation. Yet even individuals who have studied trigonometry and calmore years of high school mathematics or more rigorous standards for the bottom of the "basic" range (NCES, 1997). culus often remain largely ignorant of common abuses of data and all too numeracy that is the key to understanding our data-drenched society. nuances of quantitative inferences. As it turns out, it is not calculus but often find themselves unable to comprehend (much less to articulate) the Common responses to this well-known problem are either to demand

equations. They need a predisposition to look at the world through mathabout commonplace issues, and to approach complex problems with conematical eyes, to see the benefits (and risks) of thinking quantitatively questions of experts, and to confront authority confidently. These are people by giving them tools to think for themselves, to ask intelligent fidence in the value of careful reasoning. Quantitative literacy empowers skills required to thrive in the modern world. Quantitatively literate citizens need to know more than formulas and

A Brief History of Quantitative Literacy

as a logical system of axioms, hypotheses, and deductions and as a tool Although the discipline of mathematics has a very ancient history—both citizens be quantitatively literate is primarily a phenomenon of the late for empirical analysis of the natural world—the expectation that ordinary served more as metaphors than as measurements. The importance of twentieth century. In ancient times, numbers, especially large numbers, quantitative methods in the lives of ordinary people emerged very slowly standardized measures of length, time, and money on their arts and in the middle ages as artists and merchants learned the value of imposing

> double-entry bookkeeping (Crosby, 1997). crafts-for example, in polyphonic music, perspective drawing, and

as the dominant form of acceptable evidence in most areas of public life the twentieth century did quantitative methods achieve their current status cal rather than religious grounds (Cohen, 1982). Only in the latter part of skeptics questioned the legitimacy of policy arguments based on empirinumeracy to support the new experiment in popular democracy, even as over risk, and over life itself. instruments through which we attempt to exercise control over nature, astrology, numerology, and eschatology, numbers have become the chief (Bernstein, 1996; Porter, 1995; Wise, 1995). Despite their origins in In colonial America, leaders such as Franklin and Jefferson promoted

ety" and "math panic" have raised public awareness of the consequences good and bad, in the widespread practice in newspapers of using charts persuade (Tufte, 1983, 1990, 1997). We see the results every day, both umes on the visual display of quantitative information reveal the At the same time, publications such as Edward Tufte's extraordinary volof innumeracy (Buxton, 1991; Paulos, 1988, 1996; Tobias, 1978, 1993). and graphs as the preferred means of presenting quantitative information. unprecedented power of quantitative information to communicate and the quantitative capacity of individuals, publications about "math anxi-As the gap has widened between the quantitative needs of citizens and

standards for school mathematics that called for all students to learn rich standards for school mathematics (NCTM, 2000). These standards and photonics). In April 2000 NCTM released a much-anticipated update of its raphy, social studies) and careers (e.g., bioscience, electronics, health care, the role of quantitative methods in education (e.g., science, history, geogand challenging mathematics. Subsequently, other standards documented responded to the changing mathematical needs of society by publishing education and about the relation of mathematics to these goals. ments have engendered considerable public debate about the goals of their interpretations in state frameworks, textbooks, curricula, and assess-In 1989 the National Council of Teachers of Mathematics (NCTM)

had been a single concept into three components: prose, document, and lives of nations, government agencies that monitor literacy divided what In recognition of the increasing importance of quantitative literacy in the

five additional competencies: resources, interpersonal, information, sysquantitative methods into courses in the arts and humanities (White, quantitative literacy (Kirsch and Jungeblut, 1986; NCES, 1993; OECD, ates (Sons, 1996), the perspectives of professionals in a variety of fields economy (Murnane and Levy, 1996), the expectations of college graduexamined the role of quantitative literacy in relation to the changing tems, and technology (SCANS, 1991). More recent publications have requirement for employment (reading, 'riting, 'rithmetic) to encompass 1981). At the same time, economists expanded the traditional "3 R's" 1995, 1998). Similar awareness led many liberal arts colleges to infuse (Forman and Steen, 1999). (Steen, 1997), and the demands of the high-performance workplace

cially about its relation to mathematics. They echo the historical zens and supporting democratic government. What we learn is that confusion than consensus about the nature of quantitative literacy, espepublications, but not clarity about its meaning. These sources reveal more there is little agreement on just what it is. although almost everyone believes quantitative literacy to be important and pay at most lip service to the role numeracy plays in informing citidichotomy of mathematics as academic and numeracy as commercial The footprints of quantitative literacy can be found throughout these

Mathematics, Statistics, and Quantitative Literacy

dents directly from arithmetic to higher mathematics. At the same time, and even calculus created a highway that led increasing numbers of stuto college, courses in algebra, geometry, trigonometry, analytic geometry, matics. As secondary schools became the transition from grammar school mathematics many foundational tools, each has its own distinctive charnewest of all, bioinformatics. Although each of these subjects shares with computer science, operations research (the science of optimization), and ics, subjects such as statistics, financial mathematics, theoretical that now includes, in addition to traditional pure and applied mathematmathematics itself expanded into a collection of mathematical sciences In the beginning, grammar schools taught arithmetic and colleges, matheacter, methodologies, standards, and accomplishments.

The methametical eciance that ordinary individuals most often

exploratory data analysis and elementary statistics into school curricula Recognizing this neglect, the American Statistical Association (ASA) and bridge from arithmetic to the subtle and fascinating world of statistics. matics places relatively little emphasis on topics designed to build a government economic report. Yet school curricula still primarily serve to Statistics underlies every clinical trial, every opinion survey, and every encounter is statistics, originally the science of the state (as in census). because they anticipated public anxiety about the term statistics.) (Project founders chose quantitative literacy rather than statistics as a title This effort, interestingly, is called the "Quantitative Literacy Project." the NCTM have cooperated for many years in a campaign to infuse more prepare students only for traditional college mathematics. School mathe-

symbol-based mathematical reasoning.) rable ability find data-based statistical reasoning more difficult than from Advanced Placement examinations suggests that students of compachallenging and rigorous as mathematical reasoning. (Indeed, evidence derived from and attached to the empirical world. Surprisingly to some, tonic realm of abstract structures, numeracy is often anchored in data logic of certainty. Unlike mathematics, which is primarily about a Platics, which is primarily about uncertainty, numeracy is often about the that employs and enhances both statistics and mathematics. Unlike statis-Quantitative literacy is more a habit of mind, an approach to problems same as mathematics, nor is it (as some fear) watered-down mathematics. ricula, quantitative literacy is not the same as statistics. Neither is it the this inextricable link to reality makes quantitative reasoning every bit as Despite its occasional use as a euphemism for statistics in school cur-

tive colleges and universities. These pressures skew school curricula in performance is reinforced by increasing demand for admission to selecsociety. The tradition of using mathematics as a filter for future academic numeracy skills nor the quantitative confidence required in contemporary bers of women and minorities, who leave high school with neither the mathematics instruction has failed many students, including large numterm learning. Few can doubt that the tradition of decontextualized offer associations that are critically important for many students' longare the essence of mathematics; on the other hand, these same details ance. On the one hand, contextual details camouflage broad patterns that Connecting mathematics to authentic contexts demands delicate bal-

functionally innumerate. directions that are difficult to justify because they leave many students

contrast, typical school mathematics problems involve simplified numuncertain procedures but require primarily elementary mathematics. In ing in the world. Typical numeracy challenges involve real data and school-based knowledge, quantitative literacy involves mathematics acturally uses appropriate skills in many different contexts. concepts. The test of numeracy, as of any literacy, is whether a person nat bers and straightforward procedures but require sophisticated abstract Whereas the mathematics curriculum has historically focused

agriculture and culinary arts (Steen, 1998, 2000). Numeracy is not just one ple contexts-in history and geography, in economics and biology, in among many subjects but an integral part of all subjects be useful for the student, numeracy needs to be learned and used in multicreates in many students a stunning absence of common number sense. To when they arise in a different context. This is an especially acute problem talization, when skills or ideas learned in one class are totally forgotten for school mathematics, in which the disconnect from meaningful contexts Educators know all too well the common phenomenon of compartmen

Elements of Quantitative Literacy

numeracy, mathematical literacy, quantitative reasoning, or sometimes way by all listeners. nuances and connotations that are not necessarily interpreted in the same just plain "mathematics." Different terms, however, convey different referred to by many different names, among them quantitative literacy, The capacity to deal effectively with the quantitative aspects of life is

educators, appeared in a British government report on mathematics education (Cockcroft, 1982): An early definition of the term numerate, widely cited by mathematics

make use of mathematical skills which enables an individual to cope utes. The first of these is an "at homeness" with numbers and an ability to We would wish the word numerate to imply the possession of two attribwith the practical demands of everyday life. The second is an ability to

> sented in mathematical terms. have some appreciation and understanding of information which is pre-

(NCES, 1993), which defined quantitative literacy as The same two themes emerged in the National Adult Literacy Survey

balancing a checkbook, completing an order form). alone or sequentially, using numbers embedded in printed material (e.g. The knowledge and skills required to apply arithmetic operations, either

much more comprehensive manner as: Survey (ILSS, 2000) currently underway defines quantitative literacy in a graphs) as document literacy. In contrast, the International Life Skills example, in payroll forms, transportation schedules, maps, tables, and related knowledge and skills required to locate and use information (for The National Center for Education Statistics (NCES) defines the closely

in order to engage effectively in quantitative situations arising in life and communication capabilities, and problem solving skills that people need An aggregate of skills, knowledge, beliefs, dispositions, habits of mind,

adopts a similar definition but calls it mathematics literacy: The Programme for International Student Assessment (PISA, 2000)

reflective citizen that individual's current and future life as a constructive, concerned and judgements and to engage in mathematics in ways that meet the needs of matics plays in the world, to make well-founded mathematical An individual's capacity to identify and understand the role that mathe-

molecules, to form a more comprehensive portrait of quantitative literacy. Here are some of these elements: break them into different elements, which may be combined, as atoms in clarify these different definitions, as well as to make them more useful, we tions"), others higher-order thinking ("well-founded judgements"). To methods in world affairs. Some emphasize basic skills ("arithmetic operaity to understand and appreciate the role of mathematical and quantitative focus on an individual's ability to use quantitative tools, others on the abil-From just these four definitions significant differences emerge. Some

check other information. Confidence is the opposite of "math anxiety"; it tively confident routinely use mental estimates to quantify, interpret, and and at ease in applying quantitative methods. Individuals who are quantitamakes numeracy as natural as ordinary language. Confidence with Mathematics. Being comfortable with quantitative ideas

importance for comprehending issues in the public realm matics, its role in scientific inquiry and technological progress, and its Cultural Appreciation. Understanding the nature and history of mathe-

are at the center traditional mathematics in that data (rather than formulas or relationships) ences, and recognizing sources of error. This perspective differs from Interpreting Data. Reasoning with data, reading graphs, drawing

get at the essence of issues. risks. Individuals with such habits of inquiry accept little at face value; they constantly look beneath the surface, demanding appropriate information to ing arguments, questioning assumptions, detecting fallacies, and evaluating Logical Thinking. Analyzing evidence, reasoning carefully, understand-

mathematics is not something done only in mathematics class but a powerproblems in everyday life. For individuals who have acquired this habit, ful tool for living, as useful and ingrained as reading and speaking Making Decisions. Using mathematics to make decisions and solve

and performance standards all depend on the specific context where the context provides meaning. Notation, problem-solving strategies. Mathematics in Context. Using mathematical tools in specific settings

measure of things confidence in estimation, and common sense in employing numbers as a Number Sense. Having accurate intuition about the meaning of numbers,

skills are adept at using elementary mathematics in a wide variety of comson is likely to encounter at home or at work. Individuals who possess these mon situations Practical Skills. Knowing how to solve quantitative problems that a per-

postsecondary education braic, geometric, and statistical tools that are required in many fields of Prerequisite Knowledge. Having the ability to use a wide range of alge-

> and grammar of mathematical symbols. reading and interpreting them, and exhibiting good sense about the syntax Symbol Sense. Being comfortable using algebraic symbols and at ease in

istics of an educated (literate) person. write, and calculate, while for others it connotes the defining characterdifferent meanings: for some it suggests a minimal capacity to read, sis on traditional mathematics. Similarly, the term literacy conveys for others the term seems too vague, suggesting a diminution of emphagesting numbers and calculation rather than reasoning and logic, while (mathematics). For some the word quantitative seems too limiting, sug-(quantitative) and what is needed for engineering and physical science (mathematics), or between what is needed for general school subjects what is needed for life (quantitative) and what is needed for education they are used to signify important distinctions—for example, between terms quantitative and mathematical are used interchangeably, but often sions that permeate discussions of quantitative literacy. Sometimes the These elements illuminate but do not resolve the linguistic confu-

educated person. century, literacy and numeracy will become inseparable qualities of an selves in any of these modern forms of communication. In the twenty-first graphic forms. In addition, they need the confidence to express themtle issues that are communicated in a collage of verbal, symbolic, and require sophistication in both literacy and numeracy to think through subpate fully in a modern democratic society. Today's well-educated citizens skills are no longer sufficient to sustain a successful career or to particiing, and calculating, the principal goals of lower schools. But these basic verbal literacy. At a fundamental level we teach the skills of reading, writporary society, quantitative literacy can be viewed as a direct analog of In terms of what is needed for active and alert participation in contem-

Expressions of Quantitative Literacy

are not the real reason for the increasing emphasis on numeracy Many manifestations are commonplace and obviously important, yet they itions but at actions, not at what numeracy is but at how it is expressed. A different way to think about quantitative literacy is to look not at defin-

Examples:

- Estimating how to split a lunch bill three ways
- Comparing price options for leasing or purchasing a car
- Reading and understanding nutrition labels
- Reconciling a bank statement and locating the sources of error
- Scaling recipes up and down and converting units of volume and
- Mentally estimating discounts, tips, and sales prices
- Understanding the effects of compound interest
- Reading bus schedules and maps

sonal ends, while others serve the goals of a democratic society. Together common in our data-driven society. Some of these serve primarily persophisticated expressions of quantitative reasoning that have become More relevant to current students and future citizens are many of the more they provide a rich portrait of numeracy in the modern world.

Citizenship

of quantitative literacy. Examples: jections, inferences, and the kind of systematic thinking that is at the heart from international economics to welfare reform-depends on data, pro-Virtually every major public issue—from health care to social security,

- Understanding how resampling and statistical estimates can improve the accuracy of a census
- Understanding how different voting procedures (e.g., runoff, approval, plurality, preferential) can influence the results of
- Understanding comparative magnitudes of risk and the significance of very small numbers (e.g., 10 ppm or 250 ppb)
- Understanding that unusual events (such as cancer clusters) can easily occur by chance alone
- Analyzing economic and demographic data to support or oppose policy proposals
- example, a decline in prices compared with a decline in the rate of Understanding the difference between rates and changes in rates, for growth of prices

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- colleges, cities, products, investments, and sports teams Understanding the behavior of weighted averages used in ranking
- Appreciating common sources of bias in surveys such as poor wording of questions, volunteer response, and socially desirable
- Understanding how small samples can accurately predict public opinion, how sampling errors can limit reliability, and how sampling bias can influence results
- Recognizing how apparent bias in hiring or promotion may be an artifact of how data are aggregated
- Understanding quantitative arguments made in voter information pamphlets (e.g., about school budgets or tax proposals)
- Understanding student test results given in percentages and quality of schools percentiles and interpreting what these data mean with respect to the

in goals colleges set forth for liberal education. Examples: culture. This aspect of quantitative literacy is most commonly articulated something of the history, nature, and role of mathematics in human literature, and art, so should they know—at least in general terms— As educated men and women are expected to know something of history,

- Understanding that mathematics is a deductive discipline in which conclusions are true only if assumptions are satisfied
- Understanding the role mathematics played in the scientific revolution and the roles it continues to play
- Understanding the difference between deductive, scientific, and statistical inference
- Recognizing the power (and danger) of numbers in shaping policy in contemporary society
- Understanding the historical significance of zero and place value in our number system
- Knowing how the history of mathematics relates to the development of culture and society
- Understanding how assumptions influence the behavior of mathematical models and how to use models to make decisions

a strong preparation in calculus. Today, other aspects of quantitative literacy (e.g., statistics and discrete mathematics) are also important in these Fields such as physics, economics, and engineering have always required that students have significant quantitative preparation. Examples: fields. Increasingly, however, other academic disciplines are requiring

- Biology requires computer mathematics (for mapping genomes), studying heredity), and calculus (for determining rates of change) statistics (for assessing laboratory experiments), probability (for
- Medicine requires subtle understanding of statistics (to assess clinical trials), of chance (to compare risks), and of calculus (to understand the body's electrical, biochemical, and cardiovascular systems)
- The social sciences rely increasingly on data either from surveys for an engineering student. statistics is as important for a social science student as calculus is and censuses or from historical or archeological records; thus
- Advances in scientific understanding of the brain have transformed psychology into a biological science requiring broad understanding of statistics, computer science, and other aspects of quantitative
- The stunning impact of computer graphics in the visual arts (film, photography, sculpture) has made parts of mathematics, especially field that formerly was relatively unquantitative. calculus, geometry, and computer algorithms, very important in a
- statistics, economic indicators) or through verification and dating of of evidence provided either by numerical data (e.g., government Interpretation of historical events increasingly depends on analysis
- Even the study of language has been influenced by quantitative and new field of computer translation logical methods, especially in linguistics, concordances, and the

Professions

sions that affect people's lives, professionals in virtually every field are now expected to be well versed in quantitative tools. Examples: As interpretation of evidence has become increasingly important in deci-

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- ments about probability to establish or refute "reasonable doubt." Lawyers rely on careful logic to build their cases and on subtle argu-
- to explain risks with sufficient clarity to ensure "informed consent." Doctors need both understanding of statistical evidence and the ability
- Social workers need to understand complex state and federal regula personal budgets. tions about income and expenses to explain and verify their clients
- School administrators deal regularly with complex issues of schedquantitative dimensions. uling, budgeting, inventory, and planning—all of which have many
- Journalists need a sophisticated understanding of quantitative issues to develop an informed and skeptical understanding of events in the (especially of risks, rates, samples, surveys, and statistical evidence)
- Chefs use quantitative tools to plan schedules, balance costs against value of ingredients, and monitor nutritional balance of meals.
- Architects use geometry and computer graphics to design structures statistics and probability to model usage, and calculus to understand engineering principles.

Personal Finance

matics curriculum. Examples: an area greatly neglected in the traditional academic track of the mathe ordinary people are faced with sophisticated quantitative issues. It is also Managing money well is probably the most common context in which

- computer equipment Understanding depreciation and its effect on the purchase of cars or
- Comparing credit card offers with different interest rates for different periods of time
- Understanding the relation of risk to return in retirement investments
- Understanding the investment benefits of diversification and income averaging
- Calculating income tax and understanding the tax implications of financial decisions
- Estimating the long-term costs of making lower monthly credit card payments

• Using the Internet to make decisions about travel plans (routes, reservations)

Understanding that there are no schemes for winning lotteries

 Choosing insurance plans, retirement plans, or finance plans for buying a house

Personal Health

As patients have become partners with doctors in making decisions about health care and as medical services have become more expensive, quantitative skills have become increasingly necessary in this important aspect of people's lives. Examples:

- Interpreting medical statistics and formulating relevant questions about different options for treatment in relation to known risks and the specifics of a person's condition
- Understanding medical dosages in relation to body weight, timing of medication, and drug interactions
- Weighing costs, benefits, and health risks of heavily advertised new drugs
- Understanding terms and conditions of different health insurance policies; verifying accuracy of bills and insurance payments
- Calibrating eating and exercise habits in relation to health
- Understanding the impact of outliers on summaries of medical data

Management

Many people need quantitative skills to manage small businesses or non-profit organizations as well as to fulfill their responsibilities when they serve on boards or committees that are engaged in running any kind of enterprise. Examples:

- Looking for patterns in data to identify trends in costs, sales, and
- Developing a business plan, including pricing, inventory, and staffing strategies for a small retail store

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- Determining the break-even point for manufacturing and sale of a new product
- Gathering and analyzing data to improve profits
- Reviewing the budget of a small nonprofit organization and understanding relevant trends
- Understanding the limitations of extrapolating from data in a fixed range
- Calculating time differences and currency exchanges in different countries

Work

Virtually everyone uses quantitative tools in some way in relation to their work, if only to calculate their wages and benefits. Many examples of numeracy on the job are very specific to the particular work environment, but some are not. Examples:

- Producing a schedule or tree diagram for a complicated project
- Researching, interpreting, and using work-related formulas
- Using spreadsheets to model different scenarios for product sales and preparing graphs that illustrate these options
- Understanding and using exponential notation and logarithmic scales of measurement
- Maintaining and using quality control charts
- Optimizing networks to develop efficient ways to plan work processes
- Understanding the value of statistical quality control and statistical process control

Skills of Quantitative Literacy

For a different and more traditional perspective on quantitative literacy, we might create an inventory of quantitative skills expected of an educated person in contemporary society. For many, a list of skills is more comforting than a list of elements or expressions because skills are more immediately recognizable as something taught and learned in school. Moreover, many people believe that skills must precede applications and

tings that are both meaningful and memorable utility. To be effective, numeracy skills must be taught and learned in setdents, skills learned free of context are skills devoid of meaning and learning suggests that this approach works very imperfectly. For most stu-Unfortunately, considerable evidence about the associative nature of that once learned, quantitative skills can be applied whenever needed.

at all, only as electives. ics from statistics and optimization that are usually offered to students, if every school mathematics program, but it also includes many newer topdictable topics from arithmetic, geometry, and algebra that are part of important for courses in quantitative literacy. This list includes precaveats—a consensus among mathematicians on skills that are especially tative literacy (Sons, 1996) offers—with suitable apologies and appendix to the Mathematical Association of America's report on quantitopics and helps examiners assess the desired balance of knowledge. An sions. A list of skills helps instructors plan curricula to cover important complements the foregoing analyses in terms of elements and expresdefinition of quantitative literacy—a third dimension, so to speak, which Nevertheless, a list of skills is a valuable enhancement to our emerging

ments and expressions of quantitative literacy. They include: In fact, many of these "elective" skills are firmly embedded in the ele-

- Arithmetic: Having facility with simple mental arithmetic; estimatindirection (combinatorics). ing arithmetic calculations; reasoning with proportions; counting by
- Data: Using information conveyed as data, graphs, and charts; tor in interpreting data. drawing inferences from data; recognizing disaggregation as a fac-
- Computers: Using spreadsheets, recording data, performing calculations, creating graphic displays, extrapolating, fitting lines or curves
- Modeling: Formulating problems, seeking patterns, and drawing understanding the impact of different rates of growth standing linear, exponential, multivariate, and simulation models: conclusions; recognizing interactions in complex systems; under-
- Statistics: Understanding the importance of variability; recognizing the differences between correlation and causation, between random-

importance (especially with large samples). small samples), and between statistical significance and practical effect and finding no statistically significant effect (especially with ized experiments and observational studies, between finding no

- Chance: Recognizing that seemingly improbable coincidences are standing the value of random samples. not uncommon; evaluating risks from available evidence; under-
- Reasoning: Using logical thinking; recognizing levels of rigor in methods of inference; checking hypotheses; exercising caution in making generalizations

when it arises in a different context (such as in a course in economics). deviation in a specific quality control setting not to recognize the concept Similarly, it is not uncommon for someone who knows how to use standard when it should be used—or just as important, when it should not be used. the formula for standard deviation) not to recognize in a real-life situation mon for a person who is familiar with a mathematical or statistical tool (e.g., traditional tools and vocabulary of mathematics. Indeed, it is not uncomstresses the use of mathematical and logical tools to solve common problems, and what we might call mathematical literacy, which stresses the ment are typical of the distinction between quantitative literacy, which courses designed to meet a so-called mathematics or quantitative require-The differences between these topics and those found on many tests or in

Quantitative Literacy in Context

its context. Numeracy has no special content of its own, but inherits its content from more like writing than like algebra, more like speaking than like history. quantitative literacy is inseparable from its context. In this respect it is In contrast to mathematics, statistics, and most other school subjects,

others. But abstraction is not the focus of numeracy. Instead. numeracy power; it is what enables methods derived in one context to be applied in in seemingly different things. Abstraction is what gives mathematics its the ladder of abstraction to see, from sufficient height, common patterns numeracy grows more horizontally than vertically. Mathematics climbs Another contrast with mathematics, statistics, and most sciences is that

clings to specifics, marshaling all relevant aspects of setting and context to reach conclusions

needs of the few who may make professional use of mathematics or staissues that are important to people in their lives and work, not by future to see and use mathematics in everything they do. Numeracy is driven by is everyone's responsibility. develop the habits of mind of a numerate citizen. Like literacy, numeracy curriculum. Only by encountering the elements and expressions of numeracy is ubiquitous, opportunities abound to teach it throughout the pedagogy and context is inseparable from content. Fortunately, because tistics. In teaching quantitative literacy, content is inseparable from numeracy in real contexts that are meaningful to them will students To enable students to become numerate, teachers must encourage them

Challenges of Quantitative Literacy

work, and health to citizenship and personal finance-confronts us with a sequences of widespread innumeracy. sion about SAT scores and AP calculus enrollments. The public seems not concern about numeracy, except for ill-informed (and innumerate) obseseven part of presidential politics. Yet there is little corresponding public importance of literacy. Campaigns for literacy are commonplace, now Americans have had decades, even centuries, to recognize the public rapidly evolving phenomenon that we understand at best imperfectly. The penetration of numeracy into all aspects of life—from education, to grasp either the escalating demands for quantitative literacy or the con-

of quantitative thinking often underestimate its importance, especially for mathematics, and public concern about mathematics education does not if they themselves do not feel comfortable with it and have a highly discurriculum, most adults do recognize the importance of mathematics even tomorrow's society. In contrast, because it has been a staple of the school sequence of innumeracy. People who have never experienced the power automatically translate into a demand for quantitative literacy. torted impression of its true nature. But as we have seen, numeracy is not Ironically, public apathy in the face of innumeracy may itself be a con-

mobilize various constituencies for whom numeracy is especially Thus a key challenge in the campaign for quantitative literacy is to

> requirements. numerate patients, just as wise public policy depends on numerate citimathematics standards, high school graduation tests, college admission acy to promote questionable products or policies). These leaders, numerate public (even if they sometimes rely on the public's innumertests, college placement tests, and (occasionally) college graduation however, naturally focus their attention on existing instruments such as zens. Educational, business, and political leaders all have a stake in a important. The quality of medical care, for example, depends on

tage point from which to view education, policy, and work. functioned in the twentieth century but as a radically transformative vantative literacy. Indeed, as the twenty-first century unfolds, quantitative instruments of educational policy to include stronger emphasis on quantibecome ever more apparent and pressing (albeit in different ways to difliteracy will come to be seen not just as a minor variation in the way we ferent groups), a second challenge is to expand these traditional If, as seems inescapable, the importance of quantitative literacy will

THE DESIGN TEAM

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believe are both timely and urgent. views but a consensus on important issues that members of the Design Team Like any committee effort, this case statement represents not unanimity of

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