(Mostly grabbed from Exam 2 Study Guide from Spring 2005 by Don Lawrence)

Exam 2 will cover material from Worksheets 11 through 21. I try to make study guides complete, but there is no guarantee -I might think of something later that I forgot to include. Also look at homeworks, quizzes, handouts, and class notes.

Topics

- Optimization
 - Locate and classify critical points in a contour diagram
 - Find critical points given a formula for f
 - Second derivative test
 - Applied max-min (you aren't required to classify your critical point in these)
 - Parametrize a constraint boundary
 - o Lagrange multipliers
 - Find Lagrange points on a constraint
 - Understand basically why setting $\nabla f = \lambda \nabla g$ finds candidates
 - Extreme value theorem, including understanding what "closed" and "bounded" mean
 - o Use limits to discuss the existence of global maxes/mins
- Integration
 - Predict the sign of a multiple integral
 - Compute a multiple integral
 - Sketch the region of integration
 - Choose or change the order of integration
 - Cylindrical coordinates and triple integrals
 - Spherical coordinates and triple integrals
- Alternative coordinates for integrals
 - Change integral between polar and Cartesian coordinates
 - Change integrals between Cartesian and spherical or cylindrical coordinates
- Chain rule
 - Chain rule diagrams
- Clairault's Theorem (Mixed partials of continuous functions are equal, or $f_{xy} = f_{yx}$)
- Graphical and algebraic computation of repeated partial derivatives like f_{xy}, f_{xx}, f_{yy}

<u>Problems</u> (Of course there are many other relevant problems in your text.) (Problems 1-4 were deleted)

- (5) Find the critical points of $f(x, y) = 2x^3 + xy^2 + 5x^2 + y^2$, and use the second derivative test to classify them as max, min, saddle, or can't tell. Then argue that f can't have a global max or min.
- (6) $\int_0^1 \int_{2x}^2 \cos(1+y^2) dy dx =$
- (7) Set up a multiple integral for finding the volume bounded by the plane z = 6 2x 3yand the coordinate planes. Do not *compute* the integral. [Hint: start by finding the line where z = 6 - 2x - 3y intersects the xy-plane.]
- (8) Find the global maximum and minimum of f(x, y) = 3x 2y on the ellipse $x^2 + 2y^2 = 44$. Name any methods and/or theorems you use.
- (9) $\int_0^1 \int_{-2}^0 \int_{-\sqrt{4-y^2}}^0 \cos(x^2 + y^2) dx dy dz =$
- (10) [10 points] Use limits to discuss the existence of global maxima and minima of $f(x, y) = x^2 + xy^4$.

(11) From the 1998 senior comps exam: Suppose $f(x, y, z) = x^2 + y^3 + 5yz$, and suppose g(t) = (a(t), b(t), c(t)) is a "vector-valued function". Suppose a(0) = 4, b(0) = 5, c(0) = 6, a'(0) = 3, b'(0) = 2, and c'(0) = 1. Let h(t) = f(g(t)). Find h'(0).

(12) Draw the following contour diagram in the first quadrant: five parallel lines with negative slope, getting farther apart as they move away from the origin, labeled 5, 4, 3, 2, and 1 as you move away from the origin. Find the signs of the first and second partial derivatives.

(13) Suppose that f(x, y) has continuous partials of all orders, and suppose that $f_{xxy} = x^2 y$,

$$f_{xyy} = xy^2$$
, and $f_{yyy} = y^3$

- (a) Find f_{yxxx} .
- (b) Argue that there can't actually be such a function f.

(14) Write down the iterated integrals with correct limits which would be necessary to compute the volume of each wedge of cheese which has a perfectly horizontal base and height but that exactly six wedges will make up a completely circular cheese slab of radius a and height h.

- (a) Now change the order of integration and show that the volume is the same.
- (b) Come up with *another* order of integration which represents the same volume.
- (c) How many times can you do this?

Math 212 Spring 2015 Exam 2 Review Sheet