

SHOW ALL YOUR WORK AND EXPLAIN EVERY ANSWERAdapted from Stewart, Section 5.3, Problem 69. Suppose h is a polynomial function such that

$$h(1) = -2, h'(1) = 2, h''(1) = 3, h(2) = 6, h'(2) = 5, h''(2) = 13$$

For each of the following expressions, evaluate it exactly (if possible). If you can not evaluate the expression, explain why

1 (a) (2.5 points) $\int_1^2 h''(s) ds = h'(s) \Big|_1^2$ Using the FTC

$$= h'(2) - h'(1)$$

$$= 5 - 2$$

$$= 3$$

1 (b) (2.5 points) $\frac{d}{dx} \int_1^2 h(s) ds = 0$

Derivative of a constant is zero.
 $\int_1^2 h(s) ds$ is just a fancy way of writing a constant

1 (c) (2.5 points) $\int_1^2 h(s) ds$

Not enough info to evaluate.
 You need $H(x)$, the anti derivative of $h(x)$, to use the FTC. $H'(x) = h(x)$
 $\int_1^2 h(s) ds = H(2) - H(1)$

1 (d) (2.5 points) $\frac{d}{dx} \int_1^x h(s) ds$

$h^*(x)$ FTC part 2

$$\frac{d}{dx} \int_a^x f(t) dt = f(x)$$