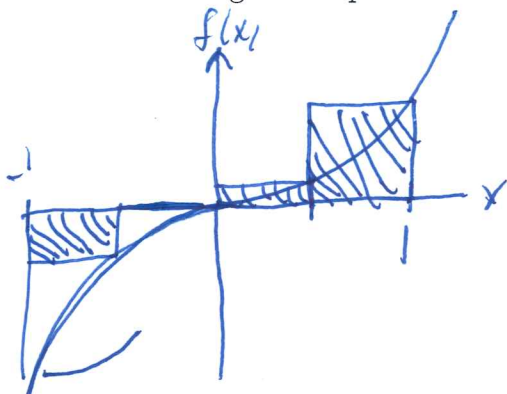


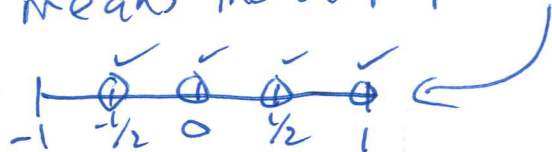
SHOW ALL YOUR WORK

- 1 (a) (6 points) Give an estimate for the value of $\int_{-1}^1 x^3 dx$ using a RIGHT HAND Riemann Sum with four rectangles of equal width. Call this value R_4 .



$$\Delta x = \frac{1 - (-1)}{4} = \frac{2}{4} = \frac{1}{2}$$

Right Hand Sum means the sample points are



$$\begin{aligned} R_4 &\approx \frac{1}{2} f(1) + \frac{1}{2} f\left(\frac{1}{2}\right) \\ &\quad + \frac{1}{2} f(0) + \frac{1}{2} f\left(-\frac{1}{2}\right) \\ &\approx \frac{1}{2} \left[1^3 + \left(\frac{1}{2}\right)^3 + 0^3 + \left(-\frac{1}{2}\right)^3 \right] \\ &\approx \frac{1}{2} \left[1 - \frac{1}{8} + 0 - \frac{1}{8} \right] \\ &= \frac{1}{2} \end{aligned}$$

- 1 (b) (4 points) Is R_4 , the estimate you computed in (a), an over-estimate or under-estimate of the exact value of $\int_{-1}^1 x^3 dx$? If you repeated your estimate with a much larger number of rectangles $N > 4$, would your estimate R_N be equal to, less than, or greater than R_4 ?

R_4 is an over estimate, which is clear from the picture (and the fact ~~over~~ that the SIGNED area represented by $\int x^3 dx$ is zero!) When $N > 4$ the estimate R_N will become more accurate so $R_N < R_4$.