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1. In this problem, just find an appropriate map; you do not need to prove it's a homeomorphism.
    - (a) Find a homeomorphism from the closed unit interval  $[0, 1]$  to  $[3, 5]$ . (Hint: First find a homeomorphism from  $[0, 1]$  to  $[0, 2]$ , and then one from  $[0, 2]$  to  $[3, 5]$ .)
    - (b) Prove that any two closed intervals  $[a, b]$  and  $[c, d]$  are homeomorphic.
    - (c) Prove that any two closed disks in  $\mathbb{R}^2$  are homeomorphic.
  2. Prove  $(0, 1) \simeq \mathbb{R}$ . Just find an appropriate map; you do not need to prove it's a homeomorphism.
  3. (a) Prove the Restriction of Continuous Maps Lemma: Let  $f : X \rightarrow Y$  be a continuous map between two topological spaces. Then for every subspace  $A \subseteq X$ , the restriction of  $f$  to  $A$ , i.e.,  $f|_A : A \rightarrow Y$ , is continuous.  
(b) Prove that if  $f : X \rightarrow Y$  is a homeomorphism, then  $\forall A \subseteq X$ ,  $f|_A : A \rightarrow f(A)$  is a homeomorphism.
  4. Separate the following into classes of homeomorphic letters.

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z

(For example, E and F are homeomorphic; so are C and W; but O and Q are not. Note that all the letters are in Sans Serif type face.)
  5. Do problem 5.6 on page 37 of Intuitive Topology.
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