The figure below is a regular hexagon ABCDEF with center O. (P, Q, R, S, T, and U are the midpoints of the sides.)



- 1. Which of the following reflections is not a symmetry of the regular hexagon?
  - a) the reflection with axis the line passing through A and D
  - b) the reflection with axis the line passing through A and B
  - c) the reflection with axis the line passing through R and S
  - d) the reflection with axis the line passing through P and Q
  - e) All of the above are symmetries of the regular hexagon.
- 2. Which of the following rotations is not a symmetry of the regular hexagon?
  - a) a 60° clockwise rotation with center O
  - b) a 180° clockwise rotation with center O
  - c) a 120° counterclockwise rotation with center O
  - d) a 90° clockwise rotation with center O
  - e) None of the above
- 3. The image of A under the reflection with axis the line passing through B and E is
  - a) Q.
  - b) D.
  - c) T.
  - d) C.
  - e) None of the above
- 4. The image of P under the reflection with axis the line passing through A and D is
  - a) R.
  - b) T.
  - c) U.
  - d) Q.
  - e) None of the above

5. The image of A under a 300° counterclockwise rotation with center O is

- a) F.
- b) C.
- c) B.
- d) E.
- e) None of the above

6. A translation sends the point A to the point C. The image of F under this translation is

- a) S.
- b) Q.
- c) D.
- d) B.
- e) None of the above
- 7. A glide reflection sends the point A to the point Q and the point P to the point D. The image of U under this glide reflection is
  - a) R.
  - b) B.
  - с) С.
  - d) P.
  - e) None of the above
- 8. A glide reflection sends the point P to the point Q and the point U to the point T. The axis of reflection for this glide reflection is
  - a) the line through T and U.
  - b) the line through R and S.
  - c) the line through C and F.
  - d) the line through P and Q.
  - e) None of the above

Translation  $T_1$  is determined by vector v and translation  $T_2$  is determined by vector w as shown below.



- 9. The image of point P under  $T_1$  followed by  $T_2$  is point
  - a) A.
  - b) B.
  - c) C.
  - d) D.
  - e) None of the above

Use the figure shown below to answer the question(s).



- 10. Triangle PAC is rotated 120° counterclockwise about the rotocenter P. The image is
  - a) triangle POA.
  - b) triangle PGO.
  - c) triangle PDE.
  - d) triangle PCD.
  - e) None of the above

Solve the problem.

- 11. The greek letter  $\Gamma$  (gamma) has symmetry type
  - a) Z<sub>1</sub>.
  - b) Z<sub>2</sub>.
  - c) D1.
  - d) D<sub>2</sub>.
  - e) None of the above

12. Which of the following letters has the same symmetry type as the letter X?

- a) E
- b) H
- c) M
- d) U
- e) None of the above

13. The symmetry type of an isosceles, nonequilateral triangle is

- a) D<sub>2</sub>.
- b) Z<sub>2</sub>.
- c) Z3.
- d) D1.
- e) None of the above

14. If an object has a 30° clockwise rotation as one of its symmetries, then it must also have as a symmetry

- a) a translation.
- b) a reflection.
- c) a 90° clockwise rotation.
- d) a 45° clockwise rotation.
- e) None of the above

- 15. If an object has a 240° clockwise rotation as one of its symmetries, then it must also have as a symmetry
  - a) a 90° counterclockwise rotation.
  - b) a 180° rotation.
  - c) a 120° clockwise rotation.
  - d) a 90° clockwise rotation.
  - e) None of the above
- 16. The result of applying three consecutive reflections with respect to two parallel axes is equivalent to a single
  - a) translation.
  - b) reflection.
  - c) glide reflection.
  - d) rotation.
  - e) None of the above

Use the figure shown below to answer the question(s).



- 17. The image of triangle OKA under a glide reflection is triangle PGE. The image of triangle OIJ under this glide reflection is
  - a) triangle PAC.
  - b) triangle OKA.
  - c) triangle DCP.
  - d) triangle PAO.
  - e) None of the above
- 18. Triangle OJK is rotated 60° clockwise about rotocenter O. The result is translated 3 units to the right. The product of this rotation and this translation is
  - a) a translation 6 units to the right
  - b) a 60° clockwise rotation having rotocenter G.
  - c) a reflection about the vertical line passing through A and G.
  - d) a 120° clockwise rotation having rotocenter O.
  - e) None of the above
- 19. Find the image of point K under a 7590° clockwise rotation about the rotocenter O.
  - a) P
  - b) G
  - c) A
  - d) L
  - e) None of the above

- 20. A rotation is formed by taking the product of a reflection about the line passing through A and I and a reflection about the line passing through A and G. The angle of this rotation is
  - a) 90°.
  - b) 45°.
  - c) 30°.
  - d) 60°.
  - e) None of the above
- 21. Point K is reflected about the line passing through points A and I. The result is then reflected about the line through G and K. The image is located at point
  - a) Ö.
  - b) J.
  - c) K.
  - d) I.
  - e) None of the above

Translation  $T_1$  is determined by vector v and translation  $T_2$  is determined by vector w as shown below.



- 22. Translation  $T_1$  followed by translation  $T_2$  determines another translation  $T_3$ . Translation  $T_3$  can be represented by the vector
  - a) z.
  - b) u.
  - c) x.
  - d) y.
  - e) None of the above
- Solve the problem.
  - 23. The result of applying the same glide reflection twice is equivalent to a single
    - a) reflection.
    - b) translation.
    - c) glide reflection.
    - d) rotation.
    - e) None of the above