- 1. Let A and B be formulas, and  $\Gamma$  a set of formulas. Suppose there is a one-line formal proof of  $\Gamma, A \vdash B$ . Show, without resorting to the Deduction Theorem, that  $\Gamma \vdash A \to B$ .
- 2. Let A and B be formulas, and  $\Gamma$  a set of formulas. Suppose there is a two-line formal proof of  $\Gamma, A \vdash B$ . Show, without resorting to the Deduction Theorem, that  $\Gamma \vdash A \to B$ .
- 3. Let A and B be formulas, and  $\Gamma$  a set of formulas. Suppose there is a three-line formal proof of  $\Gamma, A \vdash B$ . Show, without resorting to the Deduction Theorem, that  $\Gamma \vdash A \to B$ .