

Closed book. Closed Notes. May only use the Definitions-Axioms-Theorems handout, with no writings on it. 20 points per problem. Please write very legibly.

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Please do not write in this area.

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1. (a) (5 points) Give the definition of the defect of a quadrilateral in hyperbolic geometry.  
(b) (15 points) Let  $ABCD$  be a quadrilateral, and let  $A-X-B$  and  $C-Y-D$ . In hyperbolic geometry, is the following true or false:  $d(ABCD) = d(AXYD) + d(BXYC)$ ? Prove your answer. ( $d$  denotes defect.)
2. (20 points) Prove Theorem 3.3: In neutral geometry, every triangle has angle sum less than or equal to  $180^\circ$ . You may use theorems prior to Theorem 3.3.