
Closed book. Closed Notes. Please write very legibly.

Please do not write in this area.

1.

2.

3.

1. (20 points) Let U and V be two convex sets.
 - (a) Is $U \cap V$ necessarily convex? Prove your answer.
 - (b) Is $U \cup V$ necessarily convex? Prove your answer.
2. (20 points) Suppose $ABCD$ is a non-self-intersecting quadrilateral such that $\angle A = \angle C$ and $\angle B = \angle D$. Prove that $ABCD$ is a parallelogram.
3. (20 points) Prove the SSS similarity criterion for triangles: Let ABC and PQR be triangles such that, with the correspondence $A \rightarrow P$, $B \rightarrow Q$, $C \rightarrow R$, corresponding sides have a constant ratio r . Prove the two triangles are similar.