

Closed book. Closed Notes. 20 points per problem. Please write very legibly.

1. (20 points) Suppose A , B , and C are noncollinear points and L is a line not containing any of them. Prove that if L intersects one of the segments of the triangle ABC , then it intersects a second one.
2. (20 points) Let ABC be a triangle. Prove that if $AB > AC$, then $m\angle C > m\angle B$. (Hint: Let D be a point between A and B such that $AD = AC$.)
3. (20 points) Let ABC be a triangle. Let P , Q , R , and S be four distinct points such that
 - (a) $PQ = BC$,
 - (b) R and S are on the same side of \overleftrightarrow{PQ} ,
 - (c) $m\angle RPQ = m\angle B$, and
 - (d) $m\angle SQP = m\angle C$.

Prove that $\overleftrightarrow{PR} \cap \overleftrightarrow{QS} \neq \emptyset$.